| UNIT I AUTOMATA FUNDAMENTALS |  |  |  |
| :---: | :---: | :---: | :---: |
| Introduction to formal proof - Additional forms of Proof - Inductive Proofs -Finite Automata DeterministicFinite Automata - Non-deterministic Finite Automata - Finite Automata with Epsilon Transitions |  |  |  |
| PART - A |  |  |  |
| Q.No | Questions | BT Level | Competence |
| 1. | Differentiate between DFA and NFA. | BTL-2 | Understand |
| 2. | Define DFA | BTL-1 | Remember |
| 3. | Define inductive proof. | BTL-1 | Remember |
| 4. | Identify NFA- $\varepsilon$ to represent $\mathrm{a}^{*} \mathrm{~b} \mid \mathrm{c}$ | BTL-1 | Remember |
| 5. | Consider the String $X=110$ and $y=0110$ find <br> i) <br> XY ii) <br> $X^{2}$ iii) YX <br> iv) $\mathrm{Y}^{2}$ | BTL-4 | Analyze |
| 6. | Describe the following language over the input set $\mathrm{A}=\{\mathrm{a}, \mathrm{b}\}$ $\mathrm{L}=\left\{\mathrm{a}^{\mathrm{n}} \mathrm{b}^{\mathrm{n}} \mid \mathrm{n}>=1\right\}$ | BTL-4 | Analyze |
| 7. | Describe what is non-deterministic finite automata and the applications of automata theory. | BTL-1 | Remember |
| 8. | Illustrate the induction principle.? | BTL-3 | Apply |
| 9. | What is proof by contradiction? | BTL-1 | Remember |
| 10. | Describe an identifier with a transition diagram (automata). | BTL-2 | Understand |
| 11. | Define $\varepsilon$-NFA | BTL-1 | Remember |
| 12. | Summarize minimization of DFA | BTL-5 | Evaluate |
| 13. | Give the non-deterministic automata to accept strings containing the substring 0101 | BTL-2 | Understand |
| 14. | Illustrate if L be a set accepted by an NFA then there exists a DFA that accepts L. | BTL-3 | Apply |
| 15. | Define the term epsilon transition. | BTL-2 | Understand |
| 16. | Summarize the extended transition function for a $\varepsilon$-NFA | BTL-5 | Evaluate |



| 6. | (i) Compose that a language L is accepted by some $\varepsilon$-NFA if and only if $L$ is accepted by some DFA. (6) <br> (ii) Consider the following $\varepsilon$-NFA. Compute the $\varepsilon$-closure of each state and find it" s equivalent DFA. (7) |  |  |  |  | BTL-6 | Create |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\varepsilon$ | a | b | C |  |  |
|  | $\rightarrow \mathrm{p}$ | ф | \{p\} | \{q\} | \{r\} |  |  |
|  | q | \{p\} | \{q\} | \{r\} | ¢ |  |  |
|  | *r | \{q\} | \{r\} | ¢ | \{p\} |  |  |
| 7. | i)Classify how a language $L$ is accepted by some DFA if $L$ is accepted by some NFA(7) <br> (ii)Convert the following NFA to its equivalent DFA.(6) |  |  |  |  | BTL-3 | Apply |
|  |  |  |  | 0 | 1 |  |  |
|  |  | p |  | \{p,q\} | \{p\} |  |  |
|  |  | q |  | \{r\} | \{r\} |  |  |
|  |  | r |  | \{s \} | ¢ |  |  |
|  |  |  |  |  |  |  |  |
| 8. | i)Construct the DFA to recognize odd number of 1's and even number 0's (7) <br> ii) Construct the DFA over $\{\mathrm{a}, \mathrm{b}\}$ which produces not more than 3 a's <br> (6) |  |  |  |  | BTL-1 | Remember |
| 9. | (i) Point out the steps in conversion of NFA to DFA and for the following convert NFA to a DFA(7) <br> (ii) Infer the following to a regular expression(6) |  |  |  |  | BTL-4 | Analyze |


| 10. | Identify and explain the algorithm for minimization of DFA.Using the above algorithm minimize the followingDFA.(13) |  |  |  |  | BTL-1 | Remember |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11. | Tabulate the difference between the NFA and DFA .Convert the following $\varepsilon$-NFA to DFA.(13) |  |  |  |  | BTL-1 | Remember |
|  | states | $\varepsilon$ | a | b | c |  |  |
|  | P | Ф | \{p\} | \{q\} | \{r\} |  |  |
|  | Q | \{p\} | \{q\} | \{r\} | $\Phi$ |  |  |
|  | ${ }^{*} \mathrm{r}$ | \{q\} | \{r\} | ¢ | \{p\} |  |  |
| 12. | (i).Describe the extended transition function for NFA ,DFA and - $\varepsilon$-NFA (6) <br> (ii) Consider the following $\varepsilon$-NFA for an identifier <br> Consider the $\varepsilon$-closure of each state and give it's equivalent DFA.(7) |  |  |  |  | BTL-2 | Understand |
| 13. | (i)Given $\sum=\{\mathrm{a}, \mathrm{b}\}$ Analyze and construct a DFA which recognizethe language $\mathrm{L}=\left\{\mathrm{b}^{\mathrm{m}} \mathrm{ab}^{\mathrm{n}}: \mathrm{m}, \mathrm{n}>0\right\}$ |  |  |  |  | BTL-4 | Analyze |
| 14. | (i) Analyze and Prove that if n is a positive integer such that $\operatorname{nmod} 4$ is 2 or 3 then $n$ is not a perfect square.(6) <br> (ii) Construct a DFA that accept the string $\{0,1\}$ that always ends with 00 (7) |  |  |  |  | BTL-4 | Analyze |
| PART - C |  |  |  |  |  |  |  |



| UNIT II REGULAR EXPRESSION AND LANGUAGES |  |  |  |
| ---: | :--- | :---: | :---: |
| Regular Expressions - FA and Regular Expressions - Proving Languages not to be regular - Closure <br> Propertiesof Regular Languages - Equivalence and Minimization of Automata. |  |  |  |
| Q.No | PART - A |  |  |
| 1. | Questions | BT Level | Competence |
| 2. | Differentiate between regular expression and regular | BTL-1 | Remember |
| 3. | Tabulate the regular expression for the following <br> L1=set of strings 0 and 1 ending in 00 | BTL-4 | Remember |
| 4. | What are the closure properties of regular languages? |  |  |
| 5. | Explaina finite automaton for the regular expression 0*1*. | BTL-2 | Understand |
| 6. | Illustrate a regular expression for the set of all the strings | BTL-1 | Remember |


| 7. | Illustrate a regular expression for the set of all the strings have odd number of 1 's R.E=1(0+11)* | BTL-3 | Apply |
| :---: | :---: | :---: | :---: |
| 8. | Compose the difference between the + closure and $*$ closure | BTL-4 | Analyze |
| 9. | Illustrate a regular expression for the set of all strings of 0 's | BTL-2 | Understand |
| 10. | What is the Closure property of regular set S.? | BTL-2 | Understand |
| 11. |  | BTL-2 | Understand |
| 12. | Find out the language generated by the regularexpression( $0+1$ )*. | BTL-5 | Evaluate |
| 13. | Name the four closure properties of RE. | BTL-1 | Remember |
| 14. | Is it true the language accepted by any NFA is different fromthe regular language? Justify your answer. | BTL-4 | Analyze |
| 15. | Show the complement of a regular language is also regular. | BTL-3 | Apply |
| 16. | Construct a DFA for the regular expression $\mathrm{aa}{ }^{\text {* }} \mathrm{b}$ *. | BTL-3 | Apply |
| 17. | State the precedence of RE operator. | BTL-5 | Evaluate |
| 18. | Construct RE for the language over the set $\mathrm{z}=\{\mathrm{a}, \mathrm{b}\}$ in which total number of a's are divisible by 3 . | BTL-6 | Create |
| 19. | Define RE. | BTL-1 | Remember |
| 20. | Create RE to describe an identifier and positive integer. | BTL-6 | Create |
| PART | - B |  |  |
| 1. | Demonstrate how the set $\mathrm{L}=\left\{\mathrm{ab}^{\mathrm{n}} / \mathrm{n}>=1\right\}$ is not aregular.(13) | BTL5 | Evaluate |
| 2. | Express that the regular languages are closed under:(13) (a)union (b)intersection(c)Kleene Closure(d)Complement(e)Difference | BTL-1 | Remember |
| 3. | Examine whether the language $\mathrm{L}=\left(0^{\mathrm{n}_{1}} 1^{\mathrm{n}} \mid \mathrm{n}>=1\right)$ is regular ornot? Justify your answer (13) | BTL-2 | Understand |
| 4. | (i) Describe a Regular Expression. Write a Regular Expression for the set of strings that consists of alternating 0'sand 1 's.(6) <br> (ii) Construct Finite Automata equivalent to the regularexpression $(a b+a)^{*}(7)$. | BTL1 | Remember |
| 5. | (i) Describe the closure properties of regular languages.(6) <br> (ii) Describe NFA with epsilon for the $\mathrm{RE}=(\mathrm{a} / \mathrm{b}) * \mathrm{ab}$ andconvert it into DFA and further find the minimized DFA.(7) | BTL1 | Remember |


| 6. | Demonstrate how the set $\mathrm{L}=\left\{\mathrm{a}^{\mathrm{n}} \mathrm{b}^{\mathrm{n}} / \mathrm{n}>=0\right\}$ is not aregular.(13) | $\begin{aligned} & \text { BTL } \\ & -3 \end{aligned}$ | $\begin{aligned} & \text { Appl } \\ & \text { y } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 7. | Verify the whether $\mathrm{L}=\{\mathrm{a} 2 \mathrm{n} \mid \mathrm{n}>=1\}$ regular (13) | $\begin{aligned} & \text { BTL } \\ & -3 \\ & \hline \end{aligned}$ | Apply |
| 8. | i) Prove The reverse of a regular language is regular (6) <br> ii) A homomorphism of regular language is regular (7) | $\begin{aligned} & \text { BTL } \\ & -4 \end{aligned}$ | Analyze |
| 9. | Discuss on regular expressions (13) | $\begin{aligned} & \text { BTL } \\ & -2 \end{aligned}$ | Understand |
| 10 | Construct NDFA for given RE using Thomson rule. (13) <br> i) $\quad a .(a+b)^{*} a b$ <br> ii) $\quad(a . b)^{*}$ <br> iii) (a+b) | $\begin{aligned} & \text { BTL } \\ & -6 \end{aligned}$ | Create |
| 11 | Explain the DFA Minimization algorithm with an example.(13) | $\begin{aligned} & \text { BTL } \\ & -1 \\ & \hline \end{aligned}$ | Remember |
| 12 | Demonstrate how the set $\mathrm{L}=\left\{\mathrm{a}^{\mathrm{n}} \mathrm{b}^{\mathrm{m}} \mid \mathrm{m}, \mathrm{n}>=1\right\}$ is not aregular.(13) | $\begin{aligned} & \text { BTL } \\ & 2 \end{aligned}$ | Understand |
| 13 | i) Prove the L1 and L2 are two languages then L1L2 isregular (7) <br> ii) Prove the L1 and L2 are two languages then L1 . L2 isregular (6) | $\begin{aligned} & \text { BTL } \\ & 4 \end{aligned}$ | Analyze |
| 14 | i) Prove the L1 and L2 are two languages then L1 U L2is regular (7) <br> ii) Prove the L1 and L2 are two languages then L1 intersection L2 is regular (6) | $\begin{aligned} & \text { BTL } \\ & -4 \end{aligned}$ | Analyze |
|  | PART-C |  |  |
|  | (i) Deduce into regular expression that denotes the languageaccepted by following DFA.(7) <br> (ii) Evaluate the equalities for the following RE and prove forthe same (8) <br> a. $b+a b^{*}+a a^{*} b+a a^{*} a b^{*}$ <br> b. $a^{*}\left(b+a b^{*}\right)$. <br> c. $a(a+b)^{*}+a \mathrm{a}(\mathrm{a}+\mathrm{b})^{*}+\mathrm{aaa}(\mathrm{a}+\mathrm{b})^{*}$ | $\begin{aligned} & \text { BTL } \\ & -5 \end{aligned}$ | Evaluate |


| UNIT III CONTEXT FREE GRAMMAR ANDLANGUAGES |  |  |  |
| :---: | :---: | :---: | :---: |
| CFG - Parse Trees - Ambiguity in Grammars and Languages - Definition of the Pushdown Automata Languages of aPushdown Automata - Equivalence of Pushdown Automata and CFG, Deterministic Pushdown Automata. |  |  |  |
| PART - A |  |  |  |
| Q.No | Questions | BT Level | Competence |
| 1. | Express the ways of languages accepted by PDA and define them? | BTL 2 | Understand |
| 2. | Summarize PDA .Convert the following CFG to PDAS aAA, A aS\|bS|a. | BTL 2 | Understand |
| 3. | Define ambiguous grammar and CFG | BTL 1 | Remember |
| 4. | Define parse tree and derivation. | BTL 1 | Remember |
| 5. | Examine the context free Grammar representing the set of Palindrome over $(0+1)^{*}$ | BTL 2 | Understand |
| 6. | Compare Deterministic and Non deterministic PDA. Is it true that non deterministic PDA is more powerful than that of deterministic PDA? Justify your answer. | BTL 2 | Understand |
| 7. | When is PDA said to be deterministic? | BTL 1 | Remember |
| 8. | Examine the string aaabbabbba for the Grammar G with $\begin{aligned} & \mathrm{S} \rightarrow \mathrm{aB} \mid \mathrm{bA} \\ & \mathrm{~A} \rightarrow \mathrm{a}\|\mathrm{aS}\| \mathrm{bAA} \\ & \mathrm{~B} \rightarrow \mathrm{~b}\|\mathrm{bS}\| \mathrm{aBB} \end{aligned}$ | BTL 5 | Evaluate |
| 9. | Examine whether a pushdown automata has a memory? | BTL 1 | Remember |
| 10. | Designequivalence of PDA and CFG. | BTL 6 | Create |
| 11. | Point out the languages generated by a PDA using final state of the PDA and empty stack of that PDA | BTL 4 | Analyze |
| 12. | Illustrate the rule for construction of CFG from given PDA | BTL 3 | Apply |
| 13. | Give a CFG forthe language of palindrome string over $\{\mathrm{a}, \mathrm{b}\}$. Write the CFG for the language, $\mathrm{L}=\left(\mathrm{a}^{\mathrm{n}} \mathrm{b}^{\mathrm{n}} \mid \geq \mathrm{n}\right)$. | BTL 5 | Evaluate |
| 14. | What is Instantaneous Descriptions ( ID ) | BTL 1 | Remember |
| 15. | Show that $\mathrm{L}=\left\{\mathrm{a}^{\mathrm{p} / \mathrm{p}}\right.$ is prime $\}$ is not context free. | BTL 3 | Apply |


| 16. | Infer the CFG for the set of strings that contains equal numberof a's and b's over $\sum=\{\mathrm{a}, \mathrm{b}\}$ | BTL 4 | Analyze |
| :---: | :---: | :---: | :---: |
| 17. | Point out the various types of grammar with example | BTL 1 | Remember |
| 18. | Illustrate the rightmost derivation $(a+b) *$ for using the grammar and also state whether a given grammar is ambiguous one or not. $\mathrm{E} \rightarrow \mathrm{E}+\mathrm{E} / \mathrm{E} * \mathrm{E} /(\mathrm{E}) / \mathrm{id}$ | BTL 3 | Apply |
| 19. | Point out the additional features a PDA has when comparedwith NFA. | BTL 4 | Analyze |
| 20. | Convince your answer of acontext free grammar for the givenexpression ( $a+b$ ) $(a+b+0+1)^{*}$ | BTL6 | Create |
| PART - B |  |  |  |
| 1. | (i) Discuss about PDA and CFL Prove the equivalence of PDAand CFL.(6) <br> (ii) If L is Context free language then prove that there existsPDA M such that $\mathrm{L}=\mathrm{N}(\mathrm{M})$. (7) | BTL 2 | Understand |
| 2. | (i) Describe the different types of acceptance of a PDA. Are they equivalent in sense of language acceptance? Justify youranswer. (7) <br> (ii) Design a PDA to accept $\left\{0^{n} 1^{n} \mid n>1\right\}$.Draw the transition diagram for the PDA and identify the instantaneous description(ID)of the PDA which accepts the string ‘0011.(6) | BTL 1 | Remember |
| 3. | (i) Identify that deterministic PDA is less powerful than non nondeterministic PDA.(7) <br> (ii) Construct a PDA accepting $\left\{a^{n} b^{m} a^{n} / m, n>=1\right\}$ by emptystack. Also tell the corresponding context-free grammar accepting the same set.(6) | BTL 1 | Remember |
| 4. | (i)Describe and draw the parse tree for the string <br> $1+2 * 3$ Given the grammar $\mathrm{G}=(\mathrm{V}, \Sigma, \mathrm{R}, \mathrm{E})$ where <br> $\mathrm{V}=\{\mathrm{E}, \mathrm{D}, 1,2,3,4,5,6,7,9,0,+,-, *, /, 9)$, <br> $\Sigma=\{1,2,3,4,5,6,7,8,9,0,+,-, *, /,()$,$\} where \mathrm{R}$ contains <br> efollowing rules : <br> E $\quad \mathrm{D}\|(\mathrm{E})\| \mathrm{E}+\mathrm{E}\|\mathrm{E}-\mathrm{E}\| \mathrm{E} / \mathrm{E}$ <br> D $0\|1\| 2 \mid \ldots 9$ <br> $\xrightarrow{(i i)} \mathrm{Le} t=(\mathrm{V}, \mathrm{T}, \mathrm{P}, \mathrm{S})$ be a Context Free Grammar then prove that if the recursive inference procedure call tells us that terminal string W is in the language of variable A , then there is a parse tree with a root A and yield w . | BTL 6 | Create |


| 5. | (i)Define Non Deterministic Push Down Automata. Is it truethat DPDA and NDPDA are equivalent in the sense oflanguage acceptance is concern? <br> Justify Your answer.(5) <br> (ii)Convert PDA to CFG.PDA is given by <br> $\mathrm{P}=(\{\mathrm{p}, \mathrm{q}\},\{0,1\},\{\mathrm{X}, \mathrm{Y}\}, \delta, \mathrm{q}, \mathrm{Z}\}, \quad \delta \quad$ is defined by $\delta(\mathrm{p}, 1, \mathrm{z})=\{(\mathrm{p}, \mathrm{XZ})\}$, <br> $\delta(\mathrm{p}, \varepsilon, \mathrm{Z})=\{\mathrm{p}, \varepsilon)\}$, <br> $\delta(\mathrm{p}, 1, \mathrm{X})=\{(\mathrm{p}, \mathrm{XX})\}$, <br> $\delta(q, 1, X)=\{(q, \varepsilon)\}$, <br> $\delta(\mathrm{p}, 0, \mathrm{X})=\{(\mathrm{q}, \mathrm{X} 0\}$ <br> $\delta(q, 0, Z)=\{(p, Z)\} \quad(8)$ | BTL 1 | Remember |
| :---: | :---: | :---: | :---: |
| 6. | (i) Define PDA. Give an Example for a language acceptedbyPDA by empty stack.(7) <br> (ii) Convert the grammarS ->0S1\|A <br> A ->1A0\|S| ginto PDA that accepts the same language by theempty stack. Check whether 0101 belongs to $\mathrm{N}(\mathrm{M})$.(6) | BTL 2 | Understand |
| 7. | (i) Analyze the theorem: If L is Context free language thenprove that there exists PDA M such that $\mathrm{L}=\mathrm{N}(\mathrm{M}) .$ <br> (7) <br> (ii) Prove that if there is PDA that accepts by the final statethen there exists an equivalent PDA that accepts by Null State.(6) | BTL 4 | Analyze |
| 8. | Solve the following grammar $\mathrm{S} \rightarrow \mathrm{aAa}\|\mathrm{bBb}\| \mathrm{B}$ <br> $\mathrm{C} \rightarrow \mathrm{S} \mid \varepsilon$ for the string abaaba. <br> Give <br> i) Left most <br> derivation(3) ii)Right <br> most derivation(3) <br> iii)Derivation <br> Tree(3) <br> iv) For the string abaabbba, find the right most derivation.(4) | BTL 5 | Evaluate |
| 9. | (i) ExamineConstruct the grammar for the following PDAM. $\mathrm{M}=(\{q 0, \mathrm{q} 1\},\{0,1\},\{\mathrm{X}, \mathrm{z} 0\}, \delta, \mathrm{q} 0, \mathrm{Z} 0, \Phi)$ and where $\delta$ is given by $\delta(\mathrm{q} 0,0, \mathrm{z} 0)=\{(\mathrm{q} 0, \mathrm{XZ} 0)\}$, $\delta(\mathrm{q} 0,0, \mathrm{X})=\{(\mathrm{q} 0, \mathrm{XX})\},$ <br> $\delta(\mathrm{q} 0,1, \mathrm{X})=\{(\mathrm{q} 1, \varepsilon)\}$, <br> $\delta(\mathrm{q} 1,1, \mathrm{X})=\{(\mathrm{q} 1, \varepsilon)\}$, <br> $\delta(\mathrm{q} 1, \varepsilon, \mathrm{X})=\{(\mathrm{q}$ <br> $1, \varepsilon)\}, \delta(\mathrm{q} 1, \varepsilon$, <br> $\mathrm{Z} 0)=\{(\mathrm{q} 1, \varepsilon)\}$. <br> (ii) Prove that if L is $\mathrm{N}(\mathrm{M} 1)$ for some PDA M1 then L isL(M2 ) for some PDA M2. (6) | BTL 3 | Apply |
| 10. | Construct a PDA that recognizes and analyzesthe language $\left\{\mathrm{a}^{\mathrm{i}} \mathrm{~b}^{\mathrm{j}} \mathrm{k}^{\mathrm{k}} \mathrm{i}, \mathrm{j}, \mathrm{k}>0 \text { and } \mathrm{i}=\mathrm{j} \text { or } \mathrm{i}=\mathrm{k}\right\} .$ <br> Explain about PDA <br> acceptance <br> i) From empty Stack to final state. (6) <br> ii) From Final state to Empty Stack. (7) | BTL 4 | Analyze |


| 11. | Examine and construct a CFG G which accepts N(M), whereM $=\left(\left\{\mathrm{q}_{0}, \mathrm{q}_{1}\right\},\{\mathrm{a}, \mathrm{b}\},\left\{\mathrm{z}_{0}, \mathrm{z}\right\}, \delta, \mathrm{q}_{0}, \mathrm{z}_{0}, \Phi\right)$ and where $\delta$ is given by $\delta\left(\mathrm{q}_{0}, \mathrm{~b}, \mathrm{z}_{0}\right)=\left\{\left(\mathrm{q}_{0}, \mathrm{zz} 0\right)\right\}$ $\delta\left(\mathrm{q}_{0}, \varepsilon, \mathrm{z}_{0}\right)=\left\{\left(\mathrm{q}_{0}, \varepsilon\right)\right\}$ <br> $\delta\left(\mathrm{q}_{0}, \mathrm{~b}, \mathrm{z}\right)=\left\{\left(\mathrm{q}_{0}, \mathrm{zz}\right)\right\}$ <br> $\delta\left(\mathrm{q}_{0}, \mathrm{a}, \mathrm{z}\right)=\left\{\left(\mathrm{q}_{1}, \mathrm{z}\right)\right\}$ <br> $\delta\left(\mathrm{q}_{1}, \mathrm{~b}, \mathrm{z}\right)=\left\{\left(\mathrm{q}_{1}, \varepsilon\right)\right.$ <br> $\delta\left(\mathrm{q}_{1}, \mathrm{a}, \mathrm{z}_{0}\right)=\left\{\left(\mathrm{q}_{0}, \mathrm{Z}_{0}\right)\right\}$ <br> Show that $a^{n} b^{n} c^{n}$ is not context free language i.e show that theset of strings of a's and b's and c's with an equal number of each is not context free(13) | BTL-1 | Remember |
| :---: | :---: | :---: | :---: |
|  | (i) Describe the PDA that accept the given CFG <br> (7)S $\rightarrow$ xaax <br> $X \rightarrow a x / b x / €$ <br> (ii) Express a PDA for the language $a^{n} b^{m} a^{n+m}(6)$ | BTL-2 | Understand |
|  | (i) Illustratea PDA for the language $\{W C W R / W €\{0,1\}\}$.(7) <br> (ii) Illustrate a CFG for the constructed PDA. (6) | BTL-3 | Apply |
| 14. | (i) Identify CFG for the language $\mathrm{L}=\left\{0^{\mathrm{i}} 1^{\mathrm{j}} 0^{\mathrm{k}} \mid \mathrm{j}>\mathrm{i}+\mathrm{k}\right\}$ (7) <br> (ii) Define derivation tree. Explain its uses with anexample.(6) | BTL-4 | Analyze |
| PART - C |  |  |  |
| 1. | (i) Design and Explaina PDA to accept each of the followinglanguage $\left\{a^{i} b^{j} c^{k} \mid i=j \text { or } j=k\right\}(7)$ <br> (ii) The set of all string with twice as many 0 's and 1 's. (8) | BTL-5 | Evaluation |
| 2. | (i) Let P be a PDA with empty stack language $\mathrm{L}=\mathrm{N}(\mathrm{P})$ and suppose that $\varepsilon$ is not in L . Designhow you would modify P so that it accepts $\mathrm{L} \mathrm{U}\{\varepsilon\}$ by empty stack.(8). <br> (ii) Design a DPDA for even length palindrome.(7) | BTL-6 | Create |
| 3. | (i) Convert the following CFG to PDA and analyze the answer(a+b) and a++. (8) <br> $\mathrm{I} \rightarrow \mathrm{a}\|\mathrm{b}\| \mathrm{Ia}\|\mathrm{Ib}\| \mathrm{I} 0 \mid \mathrm{I}$ <br> 1 <br> $\mathrm{E} \rightarrow \mathrm{I}\|\mathrm{E}+\mathrm{E}\| \mathrm{E} * \mathrm{E} \mid$ <br> (E) <br> (ii) Convert the following CFG to PDA by empty stack.(7)S $\rightarrow 0 \mathrm{~S} 1 / \mathrm{A}$; <br> $\mathrm{A} \rightarrow 1 \mathrm{~A} 0 / \mathrm{S} / \varepsilon$ Infer whether 0101 belongs to $\mathrm{N}(\mathrm{M})$. | BTL-4 | Analyze |
| 4. | (i)If L is a CFL then prove that there exists PDA M, such thatL=N(M), language accepted by empty stack. (7) (ii)Construct a PDA empty store , $\mathrm{L}=\left\{\mathrm{a}^{\mathrm{m}} \mathrm{b}^{\mathrm{n}} \mid \mathrm{n}<\mathrm{m}\right\}$.(8) | BTL-6 | Create |


| UNIT IV PROPERTIES OF CONTEXT FREE LANGUAGES |  |  |  |
| :---: | :---: | :---: | :---: |
| Normal Forms for CFG - Pumping Lemma for CFL - Closure Properties of CFL - Turing Machines -Programming Techniques for TM. |  |  |  |
| PART - A |  |  |  |
| Q.No | Questions | $\begin{gathered} \text { BT } \\ \text { Level } \end{gathered}$ | Competence |
| 1. | Conclude the procedure for converting CNF to GNF with anexample | BTL 2 | Understand |
| 2. | Illustrate the Basic Turing Machine model and explain in onemove. What are the actions take place in TM? | BTL 3 | Apply |
| 3. | Define the two normal forms of CFG | BTL 1 | Remember |
| 4. | Point out the hierarchy summarized in the Chomskyhierarchy.. | BTL 4 | Analyze |
| 5. | Define the pumping Lemma for CFLs | BTL1 | Remember |
| 6. | Define Turing Machine. | BTL1 | Remember |
| 7. | Discuss the applications of Turing machine. | BTL 2 | Understand |
| 8. | Define Chomskian hierarchy of language. | BTL 1 | Remember |
| 9. | What is the class of language for which the TM has both accepting and rejecting configuration? Can this be called a Context free Language? Discuss. | BTL 2 | Understand |
| 10. | Show the following grammar into an equivalent one with nounit productions and no useless symbols $\begin{aligned} & \mathrm{S} \rightarrow \mathrm{ABA} \\ & \mathrm{~A} \rightarrow \mathrm{aAA}\|\mathrm{aBC}\| \end{aligned}$ <br> bB $\mathrm{B} \rightarrow \mathrm{~A}\|\mathrm{bB}\| \mathrm{Cb}$ $\mathrm{C} \rightarrow \mathrm{CC} \mid \mathrm{cC}$ | BTL 3 | Apply |
| 11. | Explain the special features of TM? Define universal TM.Define Instantaneous description of TM | BTL 5 | Evaluate |
| 12. | Define GNF. | BTL 1 | Remember |
| 13. | Prepare the difference between finite automata and turingmachine. | BTL 6 | Create |
| 14. | List the three ways to simplify a context free grammar. Whatare the properties of the CFL generated by a CFG? | BTL 5 | Evaluate |
| 15. | Draw a transition diagram for a Turing machine to identify $\mathrm{n} \bmod 2$. | BTL 1 | Remember |
| 16. | Express the techniques for TM construction. | BTL 2 | Understand |
| 17. | Develop the short notes on two-way infinite tape TM. | BTL 6 | Create |
| 18. | Differentiate TM and PDA. | BTL 4 | Analyze |
| 19. | Point outthe role of checking off symbols in a Turing Machine | BTL 4 | Analyze |
| 20. | Illustrate Halting Problem. | BTL 3 | Apply |


| PART - B |  |  |  |
| :---: | :---: | :---: | :---: |
| 1. | Express the following grammar G into Greibach NormalForm(GNF) (13) $\mathrm{S} \rightarrow \mathrm{XA} \mid \mathrm{BB}$ <br> B <br> $\rightarrow \mathrm{b} \mid$ <br> SB <br> $\mathrm{X} \rightarrow$ <br> b <br> $\mathrm{A} \rightarrow$ <br> a | BTL 1 | Remember |
| 2. | Use the CFL pumping lemma to show how each of these languages not to be context-free $\left\{a^{i^{i}} b^{j} c^{k} \mid i<j<k\right\}$ (13) | BTL 2 | Understand |
| 3. | (i) Discussa TM to accept the language $\mathrm{LE}=\left\{1^{\mathrm{n}} 2^{\mathrm{n}} 3^{\mathrm{n}} \mid \mathrm{n}\right.$ $>=1\}(6)$ <br> (ii) Construct a turing machine that estimate unarymultiplication (Say 111 X $11=11111$ ) (7) | BTL 2 | Understand |
| 4. | (i) Illustrate the Turing machine for computing $\mathrm{f}(\mathrm{m}$, $\mathrm{n})=\mathrm{m}-\mathrm{n}$ ( proper subtraction). (7) <br> (ii) Demonstrate a Turing Machine to compute $\mathrm{f}(\mathrm{m}+\mathrm{n})=\mathrm{m}+\mathrm{n}, \mathrm{m}, \mathrm{n}>=0$ and simulate their action on the input 0100. (6) | BTL 3 | Apply |
| 5. | (i) Examinethe role of checking off symbols in a TuringMachine.(6) <br> (ii) Describe a Turing Machine M to implement the function"multiplication" using the subroutine copy(7) | BTL 1 | Remember |
| 6. | (i) Demonstrate the implications of halting problem.(7) <br> (ii) Show that if a language is accepted by a multitapeturingmachine, it is accepted by a single-tape TM .(6) | BTL 3 | Apply |
| 7. | (i) Summarize in detail about multihead and multitape TMwith an example.(7) <br> (ii) Construct a Turing Machine to accept palindromes in analphabet set $\sum=\{\mathrm{a}, \mathrm{b}\}$. Trace the strings "abab" and "baab".(6) | BTL 5 | Evaluate |
| 8. | (i) Explain the TM as computer of integer function with anexample.(7) <br> (ii) Design a TM to implement the function $\mathrm{f}(\mathrm{x})=\mathrm{x}+1$. (6) | BTL 4 | Analyze |
| 9. | (i) Design a TM to accept the set of all strings $\{0,1\}$ with 010as substring.(7) <br> (ii) Write shot notes on Two -way infinite tape TM.(6) | BTL 6 | Create |
| 10. | (i)Describe computing a partial function with a TM.(6) (ii)Design a TM to accept the language $\mathrm{LE}=\left\{\mathrm{a}^{\mathrm{n}} \mathrm{b}^{\mathrm{n}} \mathrm{c}^{\mathrm{n}} \mid \mathrm{n}\right.$ $>1\}$.(7) | BTL 1 | Remember |
| 11. | (i) Define Turing machine for computing $\mathrm{f}(\mathrm{m}$, $\mathrm{n})=\mathrm{m} * \mathrm{n}, \mathrm{n} \in \mathrm{N}$. (7) <br> (ii) Write notes on Partial solvability.(6) | BTL-1 | Remember |
| 12. | (i) Construct a TM to reverse the given string \{abb\}. (6) (ii) Explain Multi tape and Multi head Turing machine withsuitable example.(7) | BTL 2 | Understand |


| 13. | (i) Analyze and Construct a TM to compute a function f(w) $=W^{\mathrm{R}}$ where $\mathrm{W} €\{\mathrm{a}, \mathrm{b}\}$.(7) <br> (ii) Construct Turing machine (TM) that replace all occurence of 111 by 101 from sequence of 0 's and 1 's.(6) | BTL 4 | Analyze |
| :---: | :---: | :---: | :---: |
| 14. | (i) Infer the Chomsky grammar classification with necessary example. (6) <br> (ii) Explain a TM with no more than three states that accepts the language. $\mathrm{a}(\mathrm{a}+\mathrm{b})^{*}$.Assume $€=\{\mathrm{a}, \mathrm{b}\}$. (7) | BTL 4 | Analyze |
| PART - C |  |  |  |
| 1. | (i) Compose the limitation of automata for Type 3, Type 2, type 0 languages.(7) <br> (ii) Consider two-tape Turing Machine (TM) and determine whether the TM always writes a nonblank symbol on its second tape during the computation on any input string ' $w$ '. Formulate this problem as a language and show it is undecidable.(8) | BTL-6 | Create |
| 2. | i) Define pumping lemma for CFL. Show that $\mathrm{L}=\left\{\mathrm{a}^{i} b^{j} \mathrm{c}^{\mathrm{k}}, \mathrm{i}<\mathrm{j}<k\right\}$ is not context free and Judge your answer.(6) <br> ii) Construct a TM to move an input string over the alphabet $\mathrm{A}=$ $\{a\}$ to the right one cell. Consider that the tape head starts somewhere on a blank cell to the left of the input string to the right one cell, leaving all the remaining cell blank.(9) | BTL-5 | Evaluate |
| 3. | (i) Design and explain a TM to compute $\mathrm{f}(\mathrm{m}, \mathrm{n})=\mathrm{m} * \mathrm{n}$, for all $\mathrm{m}, \mathrm{n} € \mathrm{~N} .(6)$ <br> (ii) Explain how a multi track in a TM can be used for testing given positive integer is a prime or $\operatorname{not}(9)$. | BTL-4 | Analyze |
| 4. | (i) Prepare a subroutine to move a TM head from its current position to the right, skipping over all 0 's until reaching a 1 or a blank. If the current position does not hold 0 , then the TM should halt. You may assume that there are no tape symbol other than 0,1 and B (blank). Then , use this subroutine to design to TM that accepts all strings of 0 's and 1 's that do not have two 1 's in a row.(8) <br> (ii) Write short notes on checking off symbols(7) | BTL-6 | Create |


| UNIT V UNDECIDABILITY |  |  |  |
| :---: | :---: | :---: | :---: |
| Non Recursive Enumerable (RE) Language - Undecidable Problem with RE - Undecidable Problems about TM -Post's Correspondence Problem, The Class P and NP |  |  |  |
| PART - A |  |  |  |
| Q.No | Questions | BT Level | Competence |
| 1. | Distinguish between PCP and MPCP? What are the conceptsused in UTMs? | BTL 2 | Understand |
| 2. | List out the features of universal turing machine. | BTL 1 | Remember |
| 3. | When a recursively enumerable language is said to be recursive? Discuss on it. | BTL 2 | Understand |
| 4. | Compare and contrast recursive and recursively enumerable Languages | BTL 4 | Analyze |
| 5. | State when a problem is said to be decidable and give anexample of an undecidable problem. | BTL 1 | Remember |
| 6. | Define NP hard and NP completeness problem. | BTL 1 | Remember |
| 7. | Define a universal language Lu? | BTL 1 | Remember |
| 8. | Is it true that the language accepted by a nondeterministicTuring Machine is different from recursively enumerable language? Judge your answer. | BTL 5 | Evaluate |
| 9. | Formulate $\begin{aligned} & \text { the two properties of } \\ & \text { recursivelyenumerable sets which are }\end{aligned}$ undecidable | BTL 6 | Create |
| 10. | When a problem is said to be decidable? Give an example ofundecidable problem. Analyze it. | BTL 4 | Analyze |
| 11. | What is (a) recursively enumerable languages (b) recursivesets? Generalize your answer. | BTL 6 | Create |
| 12. | Define the classes of P and NP. | BTL 1 | Remember |
| 13. | Is it true that complement of a recursive language is recursive? <br> Discuss your answer | BTL 2 | Understand |
| 14. | Describe an example of an undecidable problem | BTL 1 | Remember |
| 15. | Point out the properties of recursive and recursive enumerable language. | BTL 4 | Analyze |
| 16. | Illustrate on Primitive Recursive Function. | BTL 3 | Apply |
| 17. | Show the Properties of Recursive Languages | BTL 3 | Apply |
| 18. | Explain about tractable problem. | BTL 5 | Evaluate |
| 19. | Describe post correspondence problem. | BTL 2 | Understand |
| 20. | Illustrate about Time and space complexity of TM. | BTL 3 | Apply |


| 1. | (i)Describe about the tractable and intractable problems.(7)(ii)Identify that "MPCP reduce to PCP".(6) |  | BTL 1 | Remember |
| :---: | :---: | :---: | :---: | :---: |
| 2. | (i) Describe about Recursive and Recursive Enumerablelanguages with example. (7) (ii) State and describe RICE theorem.(6) |  | BTL 1 | Remember |
| 3. | (i) Summarize diagonalization language. (6) <br> (ii) Discuss the significance of universal turing machine and also construct a turing machine to add two numbers and encodeit .(7) |  | BTL 2 | Understan d |
| 4. | Discuss post correspondence problem Let $\sum=\{0,1\}$. Let A andB be the lists of three strings each , defined as |  | BTL 2 | Understan <br> d |
|  | List A | List B |  |  |
|  | wi | xi |  |  |
|  | 1 | 111 |  |  |
|  | 2 10111 | 10 |  |  |
|  | 3 10 | 0 |  |  |
|  | (i) Does the PCP have a solution?(7) <br> (ii) Prove that the universal language is recursivelyenumerable.(6) |  |  |  |
| 5. | (i)Explain computable functions with suitable example.(6)(ii)Explain in detail notes on Unsolvable Problems.(7) |  | BTL 4 | Apply |
| 6. | (i) Describe in detail notes on universal Turing machines withexample.(7) <br> (ii) Collect and write the short notes on NPcompleteproblems.(6) |  | BTL 1 | Remember |
| 7. | (i) Show that the diagonalization language $\left(\mathrm{L}_{\mathrm{d}}\right)$ is not arecursively enumerable.(7) <br> (ii) Illustrate about unsolvability.(6) |  | BTL 3 | Apply |
| 8. | (i)Compare the difference between recursive and recursively <br> enumerable <br> languages.(7) <br> (ii)Explain about <br> PCP.(6) |  | BTL 5 | Evaluate |
| 9. | (i) Explain about Universal Turing machine and show that theuniversal language $\left(\mathrm{L}_{u}\right)$ is recursively enumerable but not recursive. Generalize your answer(8) <br> (ii) Design and explain how to measure and classifycomplexity.(5) |  | BTL 6 | Create |
| 10. | (i) Explain about the recursively Enumerable Language withexample.(6) <br> (ii) Point out that the following problem is undecidable.Given two CFGs G1 and G2 is $\mathrm{L}(\mathrm{G} 1) \cap \mathrm{L}(\mathrm{G} 2)=\varnothing$.(7) |  | BTL 4 | Analyze |
| 11. | (i) Show that the characteristic function of the set of all evennumber is recursive .(7) <br> (ii) Illustrate in detail notes on primitive recursive functionswith examples.(6) |  | BTL-3 | Apply |


| 12. | (i)Point out the Measuring and Classifying Complexity.(7) <br> (ii)Does PCP with two lists $\mathrm{x}=\left(\mathrm{b}, \mathrm{b} \quad \mathrm{ab}^{3}, \mathrm{ba}\right)$ and $y=\left(b^{3}, b a, a\right)$ <br> have a solution. Analyze your answer.(6) | BTL4 | Analyze |
| :---: | :---: | :---: | :---: |
| 13. | (i) Discuss in detail about Time and Space Computing of aTuring Machine(6) <br> (ii) Express two languages which are not recursivelyenumerable.(7) | $\begin{gathered} \text { BTL- } \\ 2 \end{gathered}$ | Understa nd |
| 14. | (i) Describe in detail Polynomial Time reduction and NP-completeness.(7) <br> (ii) List out the short notes on NP-Hard Problems.(6) | $\begin{gathered} \text { BTL } \\ 1 \end{gathered}$ | Rememb er |
| PART-C |  |  |  |
| 1. | Consider and find the languages obtained from the followingoperations: <br> (i) Union of two recursive languages.(5) <br> (ii) Union of two recursively enumerable languages.(5) <br> (iii) L if L and complement of L are recursively enumerable.(5) | $\begin{gathered} \text { BTL } \\ 5 \end{gathered}$ | Evaluate |
| 2. | Prove that the universal language is recursively enumerable butnot recursive. Generalize your answer.(15) | $\begin{gathered} \text { BTL- } \\ 6 \end{gathered}$ | Create |
| 3. | (i) Plan and explain on decidable and un-decidable problemswith an example(7) <br> (ii) Design and prove that for two recursive languages L1 andL2 their union and intersection is recursive.(8) | $\begin{gathered} \text { BTL- } \\ 6 \end{gathered}$ | Create |
| 4. | (i) Compare and write about tractable and untractactable problems with an example.(10) <br> (ii) Explain the language $\mathrm{L}_{\mathrm{u}}$ and show that $\mathrm{L}_{\mathrm{u}}$ is RElanguage.(5) | $\begin{gathered} \text { BTL- } \\ 4 \end{gathered}$ | Analyze |

