

CE8491

SOIL MECHANICS ▶ .



UNIT – 1
BASICS OF SOIL MECHANICS

Out line

Topics for discussion

1. Origin of Soils
2. Three Phase Diagram
3. Important Terms
4. Phase Relationships
5. Atterberg's limits

Origin of Soils

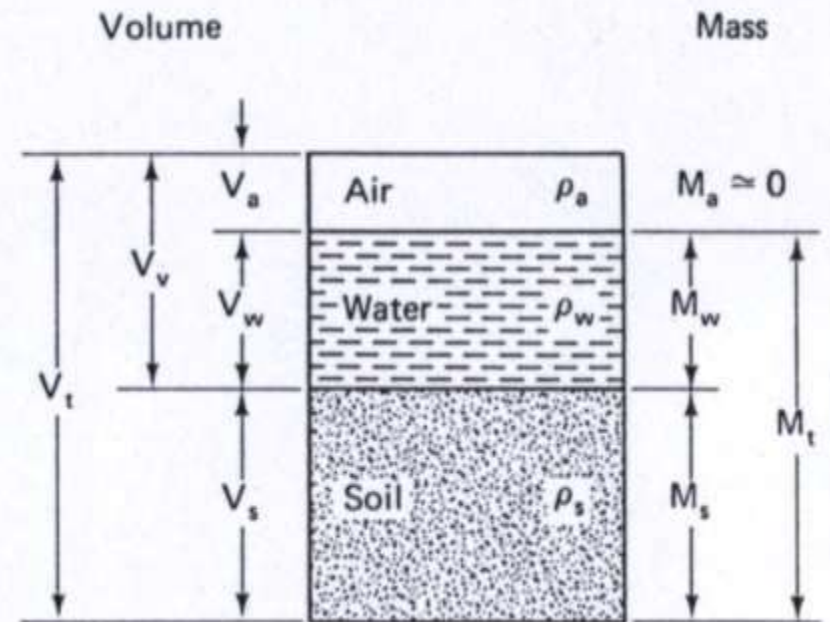
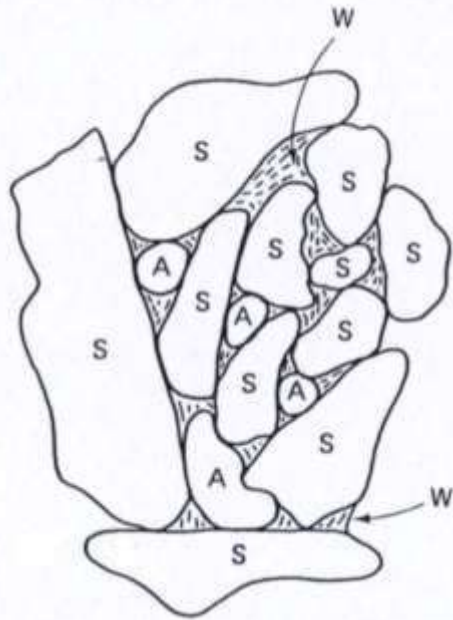
- Soils are formed by weathering of rocks due to mechanical disintegration or chemical decomposition.
- Exposed rocks are eroded and degraded by various physical and chemical processes.
- The products of erosion are picked up and transported to some other place by wind water etc.
- This shifting of material disturbs the equilibrium of forces on the earth and causes large scale movements and upheavals.

Types of Soils

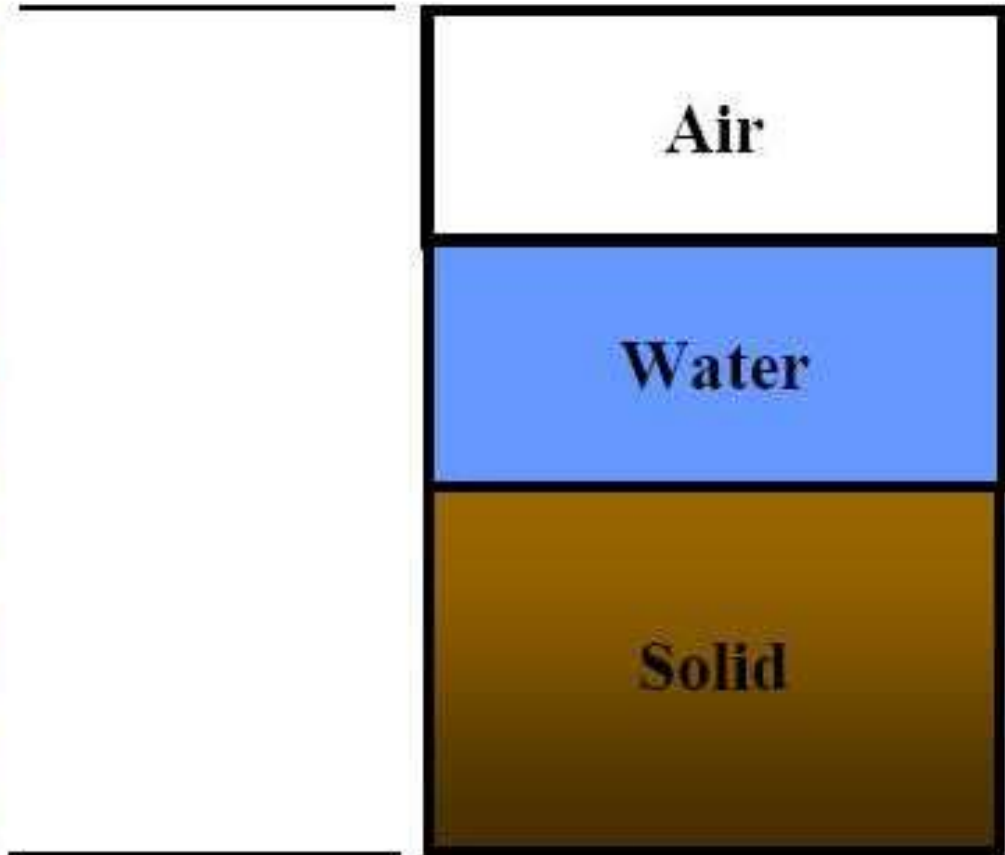
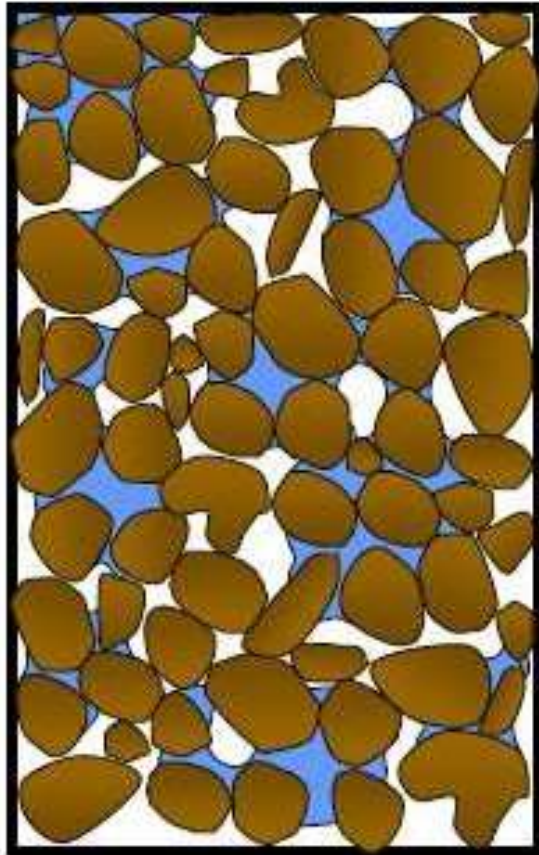
- (1) **Glacial soils:** formed by transportation and deposition of glaciers.
- (2) **Alluvial soils:** transported by running water and deposited along streams.
- (3) **Lacustrine soils:** formed by deposition in quiet lakes (e.g. soils in Taipei basin).
- (4) **Marine soils:** formed by deposition in the seas (Hong Kong).
- (5) **Aeolian soils:** transported and deposited by the wind (e.g. soils in the loess plateau, China).
- (6) **Colluvial soils:** formed by movement of soil from its original place by gravity, such as during landslide (*Hong Kong*). (from Das, 1998)

Three Phases in Soils

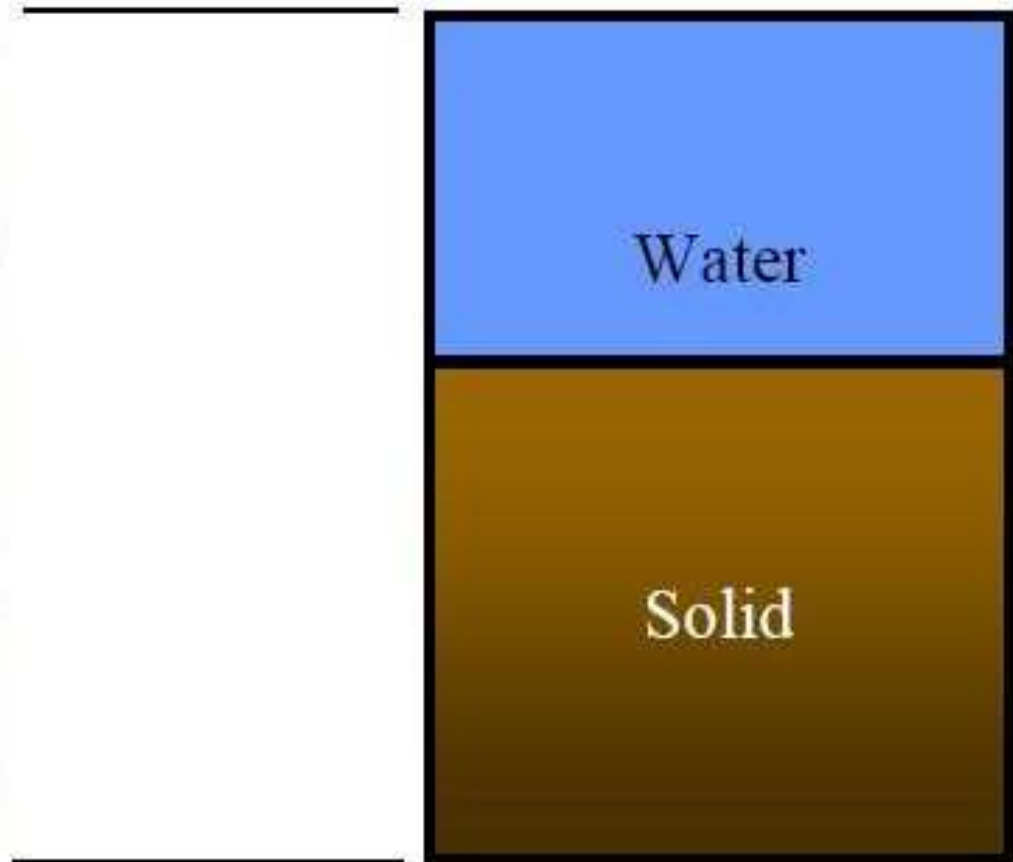
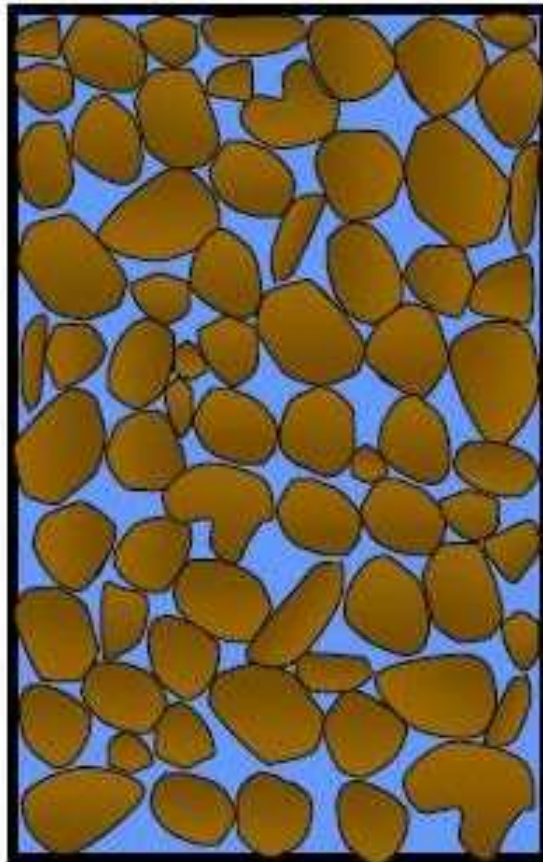
S : Solid Soil particle
W: Liquid Water (electrolytes)
A: Air Air



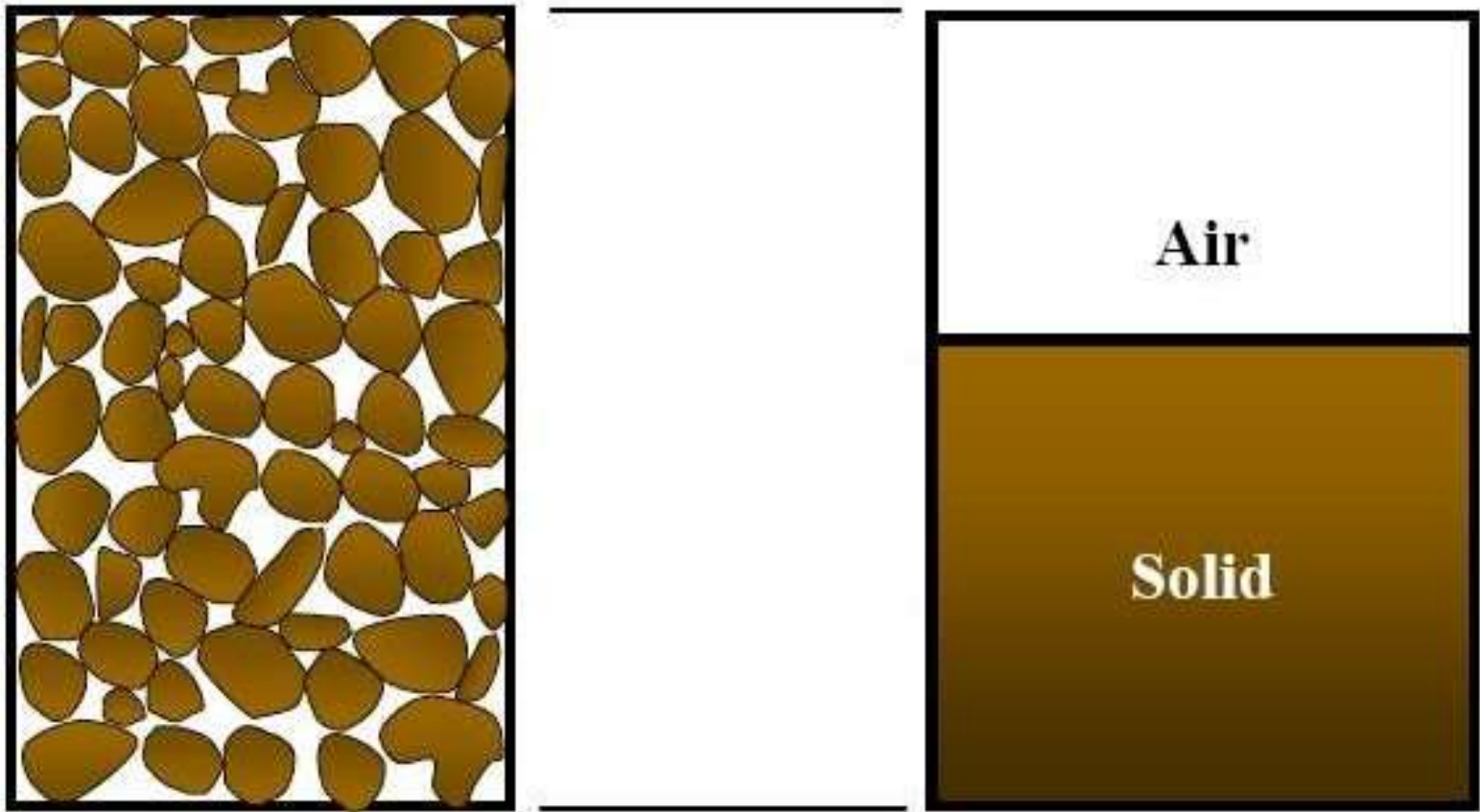
Three Phase Diagram



Fully Saturated Soils (**Two** phase)

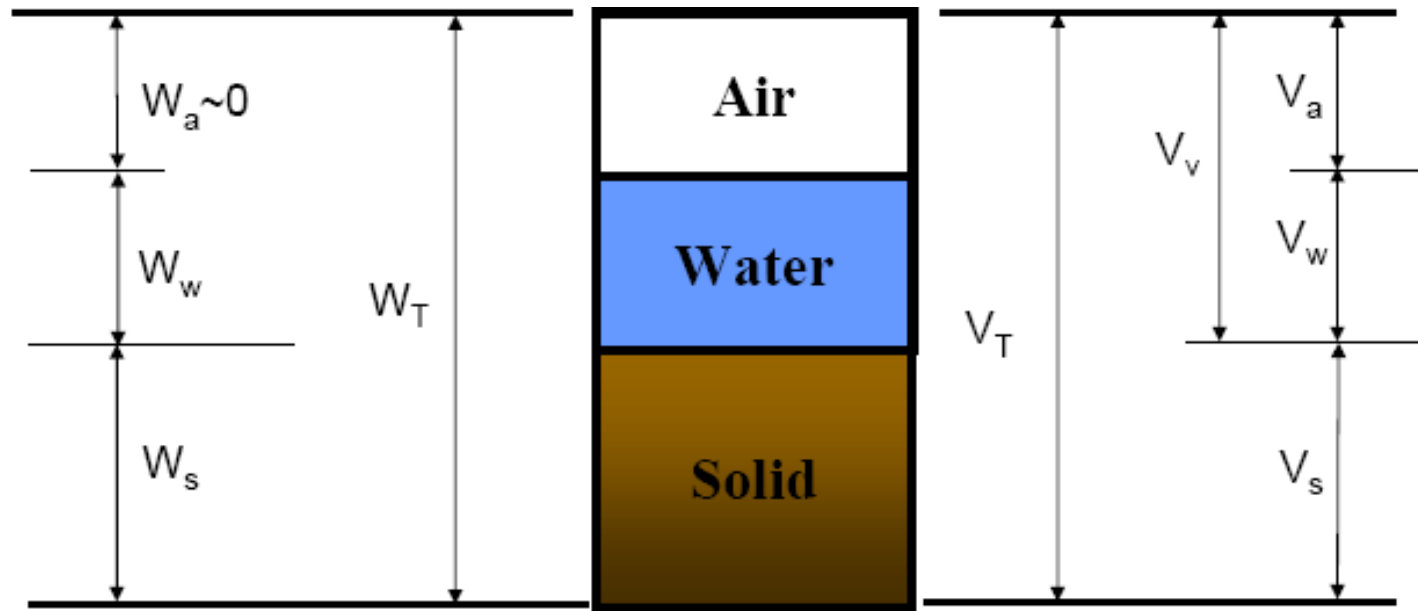


Dry Soils (**Two** phase) [Oven Dried]



PHASE DIAGRAM

For purpose of study and analysis, it is convenient to represent the soil by a **PHASE DIAGRAM**, with part of the diagram representing the solid particles, part representing water or liquid, and another part air or other gas.



W_t : total weight

W_s : weight of solid

W_w : weight of water

W_a : weight of air = 0

V_t : total volume

V_s : volume of solid

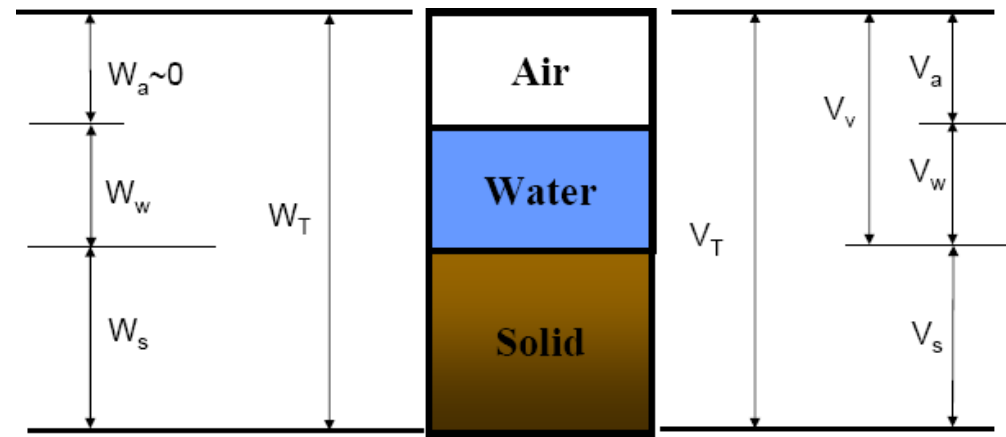
V_w : volume of water

V_v : volume of the void

Volumetric Ratios

(1) Void ratio e

$$e = \frac{\text{Volume of voids}}{\text{Volume of solids}} = \frac{V_v}{V_s}$$



(2) Porosity $n\%$

$$n = \frac{\text{Volume of voids}}{\text{Total volume of soil sample}} = \frac{V_v}{V_t} \times 100$$

(3) Degree of Saturation $S\%$ (0 - 100%)

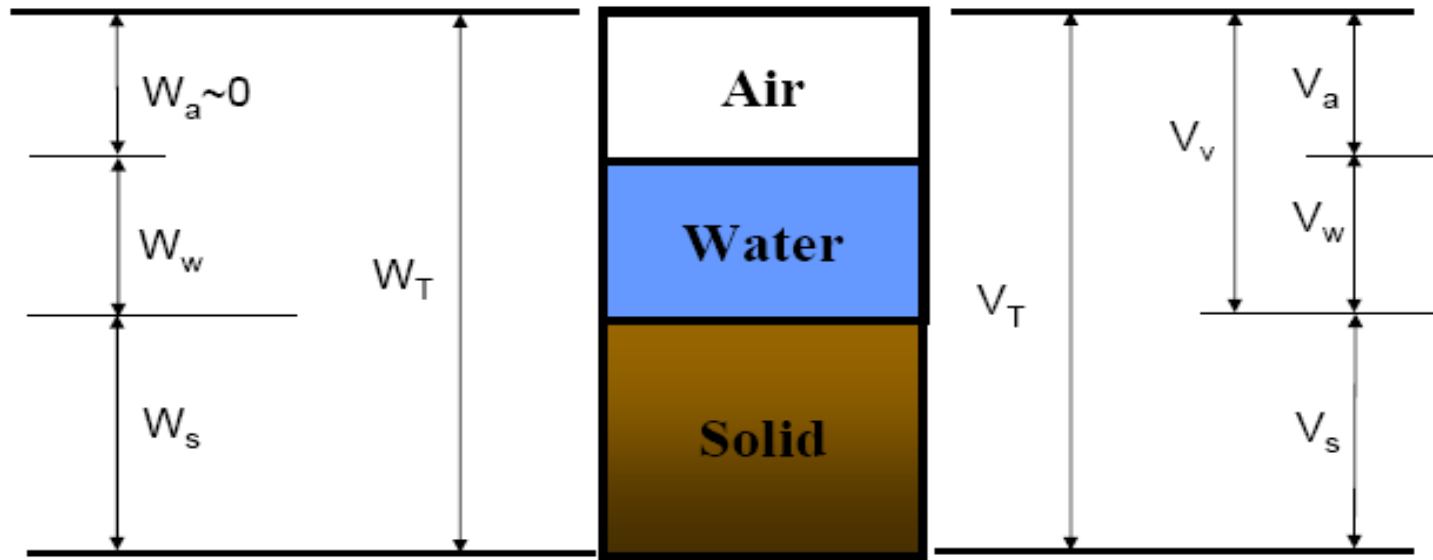
$$S = \frac{\text{Total volume of voids contains water}}{\text{Total volume of voids}} = \frac{V_w}{V_v} \times 100\%$$

Dry

Saturated

Weight

Portion



(1) Water Content $w\%$

$$w = \frac{\text{Weight of water}}{\text{Weight of soil solids}} = \frac{W_w}{W_s} \cdot 100\%$$

Soil unit weights

(1) Dry unit weight

$$\gamma_d = \frac{\text{Weight of soil solids}}{\text{Total volume of soil}} = \frac{W_s}{V_t}$$

(2) Total, Wet, Bulk, or Moist unit weight

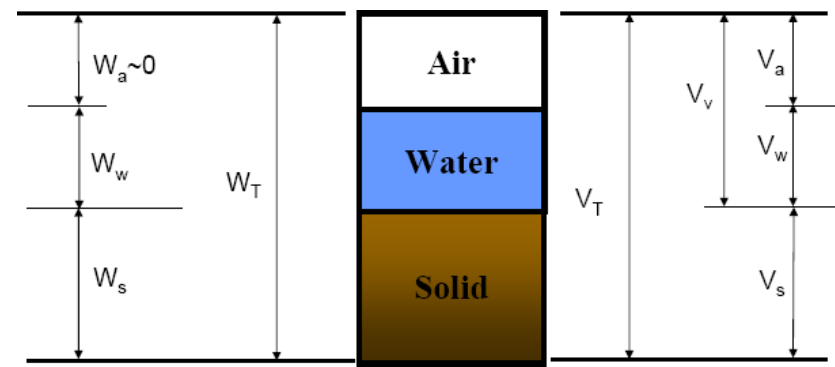
$$\gamma = \frac{\text{Total weight of soil}}{\text{Total volume of soil}} = \frac{W_s + W_w}{V_t}$$

(3) Saturated unit weight (considering $S=100\%$, $V_a=0$)

$$\gamma_{sat} = \frac{\text{Weight of soil solids + water}}{\text{Total volume of soil}} = \frac{W_s + W_w}{V_t}$$

(4) Submerged unit weight

$$\gamma' = \gamma_{sat} - \gamma_w$$



Note: The density/or unit weight are ratios which connects the volumetric side of the PHASE DIAGRAM with the mass/or weight side.

Specific gravity, G_s

The ratio of the weight of solid particles to the weight of an equal volume of distilled water at 4°C

$$G_s = \frac{w_s}{V_s \gamma_w}$$

i.e., the specific gravity of a certain material is ratio of the unit weight of that material to the unit weight of water at 4°C.

The specific gravity of soil solids is often needed for various calculations in soil mechanics.

$$G_s = \frac{\gamma_s}{\gamma_w}$$

- $G_w = 1$
- $G_{\text{mercury}} = 13.6$

- Expected Value for G_s

Type of Soil	G_s
Sand	2.65 - 2.67
Silty sand	2.67 – 2.70
Inorganic clay	2.70 – 2.80
Soils with mica or iron	2.75 – 3.00
Organic soils	< 2.00

Relationships Between Various Physical Properties

All the weight- volume relationships needed in soil mechanics can be derived from appropriate combinations of six fundamental definitions. They are:

- 1. Void ratio**
- 2. Porosity**
- 3. Degree of saturation**
- 4. Water content**
- 5. Unit weight**
- 6. Specific gravity**

1. Relationship between e and n

$$e = \frac{V_v}{V_s} = \frac{V_v}{V - V_v} = \frac{\left(\frac{V_v}{V}\right)}{1 - \left(\frac{V_v}{V}\right)} = \frac{n}{1 - n} \quad (3.6)$$

Also, from Eq. (3.6),

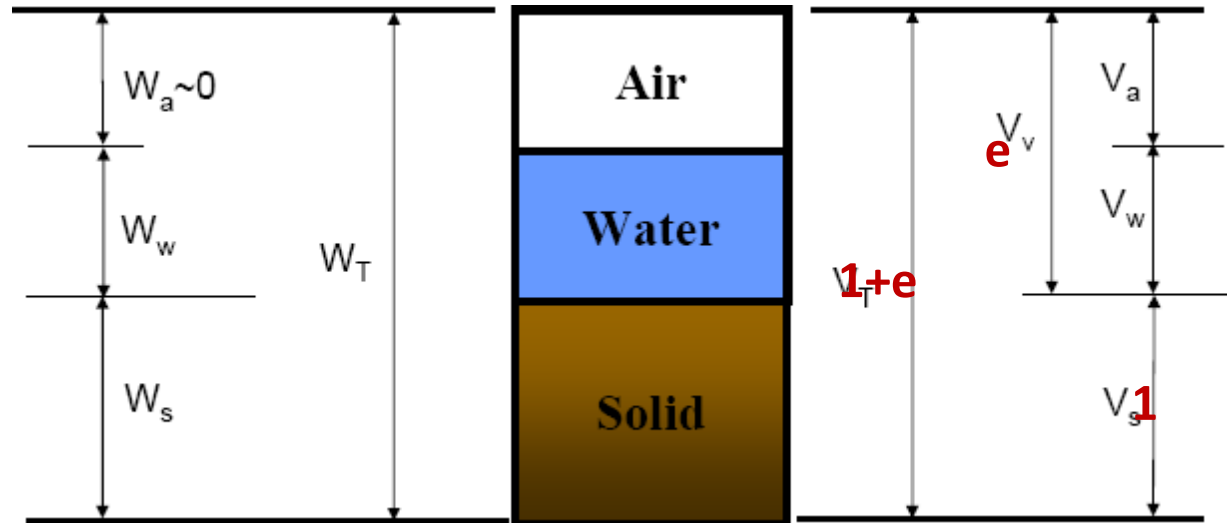
$$n = \frac{e}{1 + e} \quad (3.7)$$

Using phase diagram

Given : e

required: n

$$n = \frac{V_v}{V_t} = \frac{e}{1 + e}$$



2. Relationship among e, S, w, and G_s

$$w = \frac{w_w}{G_s V_s} = \frac{\gamma_w V_w}{V_w w_s \gamma_s V_s} = \frac{\gamma_w}{G_s V_s}$$

• Dividing the denominator and numerator of the R.H.S. by V_v yields:

$$Se = w G_s$$

• This is a very useful relation for solving THREE-PHASE RELATIONSHIPS.

3. Relationship among γ , e , S and G_s

$$\gamma = \frac{W}{V} = \frac{W_w + W_s}{V_s + V_v} = \frac{\gamma_w V_w + \gamma_s V_s}{V_s + V_v} = \frac{\gamma_w V_w + \gamma_w G_s V_s}{V_s + V_v}$$

$$\gamma = \frac{\gamma_w V_w + \gamma_w G_s V_s}{V_s + V_v}$$

$$\gamma = \frac{\gamma_w (S_o + C)}{1 + e}$$

• Notes:

- Unit weights for dry, fully saturated and submerged cases can be derived from the upper equation
- Water content can be used instead of degree of saturation.

Method to solve Phase Problems

Method : Memorize relationships

$$Se = wG_s$$

$$\gamma = \frac{(Se + G_s)}{1 + e} \gamma_w$$

$$n = \frac{e}{1 + e}$$

$$\gamma_d = \frac{\gamma}{1 + w}$$

Example

1

The moist unit weight of a soil is 19.2 kN/m^3 . Given that $G_s = 2.69$ and $w = 9.8\%$, determine

- a. Dry unit weight
- b. Void ratio
- c. Porosity
- d. Degree of saturation

$$\text{a. } \gamma_d = \frac{\gamma}{1 + w} = \frac{19.2}{1 + \frac{9.8}{100}} = \mathbf{17.5 \text{ kN/m}^3}$$

$$\text{b. } \gamma_d = 17.5 = \frac{G_s \gamma_w}{1 + e} = \frac{(2.69)(9.81)}{1 + e}; \quad e = \mathbf{0.51}$$

$$\text{c. } n = \frac{e}{1 + e} = \frac{0.51}{1 + 0.51} = \mathbf{0.338}$$

$$\text{d. } S = \frac{w G_s}{e} = \frac{(0.098)(2.69)}{0.51} \times 100 = \mathbf{51.7\%}$$

Field density testing (e.g., sand replacement method) has shown bulk density of a compacted road base to be 2.06 g/cc with a water content of 11.6%. Specific gravity of the soil grains is 2.69. Calculate the dry density, porosity, void ratio and degree of saturation.

Solution:

$$w = \frac{Se}{G_s}$$

e 2

$$\therefore Se = (0.116)(2.69) = 0.312$$

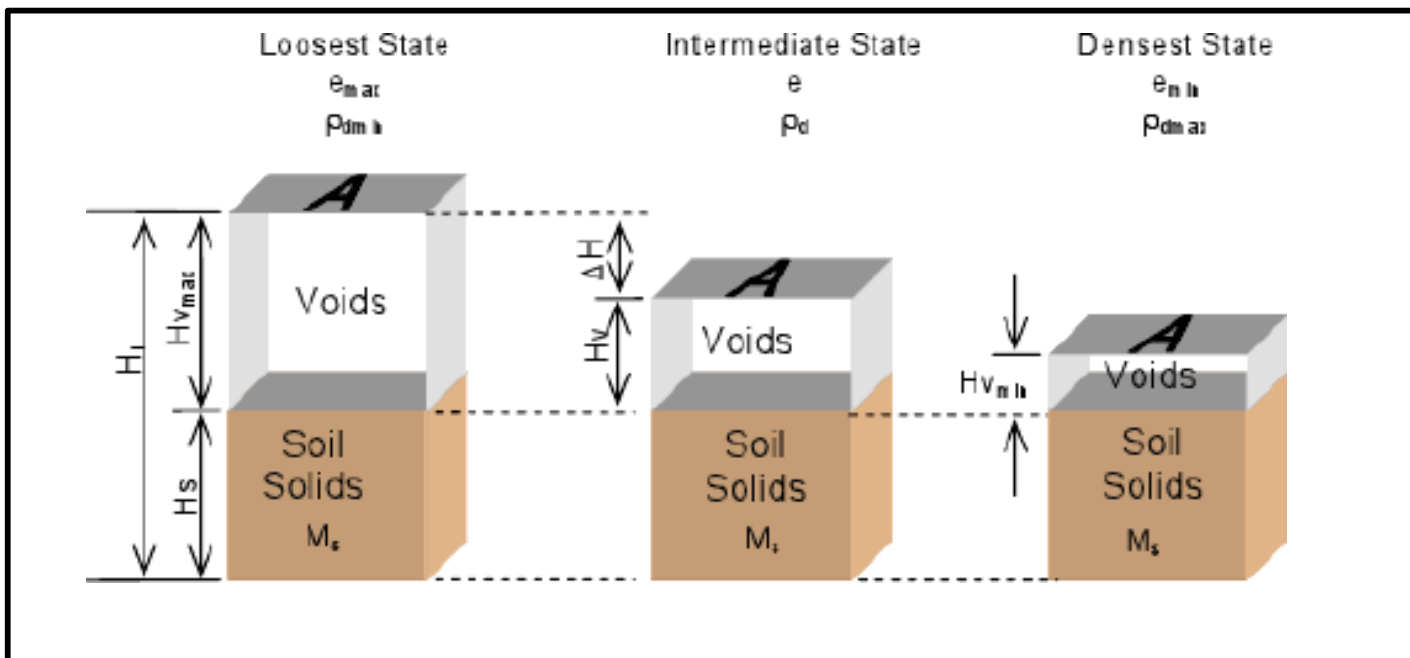
$$\rho_m = \frac{G_s + Se}{1 + e} \rho_w$$

$$\therefore 2.06 = \frac{2.69 + 0.312}{1 + e} \times 1.0$$

$$\therefore e = 0.457$$

• Relative Density

- The **relative density** is the parameter that compares the volume reduction achieved from **compaction** to the maximum possible volume reduction
- The relative density D_r , also called **density index** is commonly used to indicate the IN SITU denseness or looseness of granular soil.



Volume reduction from compaction of granular soil

- D_r can be expressed either in terms of **void ratios** or **dry densities**.

$$D_r = \frac{e_{\max} - e}{e_{\max} - e_{\min}}$$

where D_r = relative density, usually given as a percentage

e = *in situ* void ratio of the soil

e_{\max} = void ratio of the soil in the loosest state

e_{\min} = void ratio of the soil in the densest state

$$D_r = \frac{\left[\frac{1}{\gamma_{d(\min)}} \right] - \left[\frac{1}{\gamma_d} \right]}{\left[\frac{1}{\gamma_{d(\min)}} \right] - \left[\frac{1}{\gamma_{d(\max)}} \right]} = \left[\frac{\gamma_d - \gamma_{d(\min)}}{\gamma_{d(\max)} - \gamma_{d(\min)}} \right] \left[\frac{\gamma_{d(\max)}}{\gamma_d} \right]$$

where $\gamma_{d(\min)}$ = dry unit weight in the loosest condition (at a void ratio of e_{\max})

γ_d = *in situ* dry unit weight (at a void ratio of e)

$\gamma_{d(\max)}$ = dry unit weight in the densest condition (at a void ratio of e_{\min})

• Remarks

- The range of values of D_r may vary from a minimum of zero for very **LOOSE** soil to a maximum of 100% for a very **DENSE** soil.
- Because of the irregular size and shape of granular particles, it is not possible to obtain a ZERO volume of voids.

- Granular soils are qualitatively described according to their relative densities as shown below

Relative Density (%)	Description of soil deposit
0-15	Very loose
15-50	Loose
50-70	Medium
70-85	Dense
85-100	Very dense

- The use of relative density has been restricted to **granular** soils because of the difficulty of determining e_{\max} in clayey soils. **Liquidity Index** in fine-grained soils is of similar use as D_r in granular soils.

ATTERBERG LIMITS

➤ Liquid limit test:

- A soil is placed in the grooving tool which consists of a brass cup and a hard rubber base.
- A groove is cut at the center of the soil pat using a standard grooving tool.
- The cup is then repeatedly dropped from a height of 10mm until a groove closure of 12.7 mm.
- The soil is then removed and its moisture content is determined.
- The soil is said to be at its liquid limit when exactly 25 drops are required to close the groove for a distance of 12.7 mm (one half of an inch)

APPARATUS



➤ **Plastic limit test:**

A soil sample is rolled into threads until it becomes thinner and eventually breaks at 3 mm.

it is defined as the moisture content in percent at which the soil crumbles when rolled into the threads of 3.0 mm.

If it is wet, it breaks at a smaller diameter; if it is dry it breaks at a larger diameter.